

$$\text{and } \theta_k(s_k) = \frac{\prod_{j=1}^{M_k} \Gamma(d_j^{(k)} - \delta_j^{(k)} s_k) \prod_{j=1}^{N_k} \Gamma(1 - c_j^{(k)} + \gamma_j^{(k)} s_k)}{\sum_{i^{(k)}=1}^{R^{(k)}} [\tau_{i^{(k)}} \prod_{j=M_k+1}^{Q_{i^{(k)}}} \Gamma(1 - d_{ji^{(k)}}^{(k)} + \delta_{ji^{(k)}}^{(k)} s_k) \prod_{j=N_k+1}^{P_{i^{(k)}}} \Gamma(c_{ji^{(k)}}^{(k)} - \gamma_{ji^{(k)}}^{(k)} s_k)]} \quad (1.3)$$

Suppose , as usual , that the parameters

$$b_j, j = 1, \dots, Q; a_j, j = 1, \dots, P;$$

$$c_{ji^{(k)}}^{(k)}, j = n_k + 1, \dots, P_{i^{(k)}}; c_j^{(k)}, j = 1, \dots, N_k;$$

$$d_{ji^{(k)}}^{(k)}, j = M_k + 1, \dots, Q_{i^{(k)}}; d_j^{(k)}, j = 1, \dots, M_k;$$

with $k = 1 \dots, r, i = 1, \dots, R, i^{(k)} = 1, \dots, R^{(k)}$

are complex numbers , and the $\alpha's, \beta's, \gamma's$ and $\delta's$ are assumed to be positive real numbers for standardization purpose such that

$$U_i^{(k)} = \sum_{j=1}^N \alpha_j^{(k)} + \tau_i \sum_{j=N+1}^{P_i} \alpha_{ji}^{(k)} + \sum_{j=1}^{N_k} \gamma_j^{(k)} + \tau_{i^{(k)}} \sum_{j=n_k+1}^{P_{i^{(k)}}} \gamma_{ji^{(k)}}^{(k)} - \tau_i \sum_{j=1}^{Q_i} \beta_{ji}^{(k)} - \sum_{j=1}^{M_k} \delta_j^{(k)} - \tau_{i^{(k)}} \sum_{j=M_k+1}^{Q_{i^{(k)}}} \delta_{ji^{(k)}}^{(k)} \leq 0 \quad (1.4)$$

The reals numbers τ_i are positives for $i = 1$ to R , $\tau_{i^{(k)}}$ are positives for $i^{(k)} = 1$ to $R^{(k)}$

The contour L_k is in the s_k -p lane and run from $\sigma - i\infty$ to $\sigma + i\infty$ where σ is a real number with loop , if necessary ,ensure that the poles of $\Gamma(d_j^{(k)} - \delta_j^{(k)} s_k)$ with $j = 1$ to m_k are separated from those of $\Gamma(1 - a_j + \sum_{i=1}^r \alpha_j^{(k)} s_k)$ with $j = 1$ to N and $\Gamma(1 - c_j^{(k)} + \gamma_j^{(k)} s_k)$ with $j = 1$ to N_k to the left of the contour L_k . The condition for absolute convergence of multiple Mellin-Barnes type contour (1.9) can be obtained by extension of the corresponding conditions for multivariable H-function given by as :

$$|arg z_k| < \frac{1}{2} A_i^{(k)} \pi, \text{ where}$$

$$A_i^{(k)} = \sum_{j=1}^N \alpha_j^{(k)} - \tau_i \sum_{j=N+1}^{P_i} \alpha_{ji}^{(k)} - \tau_i \sum_{j=1}^{Q_i} \beta_{ji}^{(k)} + \sum_{j=1}^{N_k} \gamma_j^{(k)} - \tau_{i^{(k)}} \sum_{j=N_k+1}^{P_{i^{(k)}}} \gamma_{ji^{(k)}}^{(k)} + \sum_{j=1}^{M_k} \delta_j^{(k)} - \tau_{i^{(k)}} \sum_{j=M_k+1}^{Q_{i^{(k)}}} \delta_{ji^{(k)}}^{(k)} > 0, \text{ with } k = 1 \dots, r, i = 1, \dots, R, i^{(k)} = 1, \dots, R^{(k)} \quad (1.5)$$

The complex numbers z_i are not zero. Throughout this document , we assume the existence and absolute convergence conditions of the multivariable Aleph-function.

We may establish the the asymptotic expansion in the following convenient form :

$$\aleph(z_1, \dots, z_r) = O(|z_1|^{\alpha_1}, \dots, |z_r|^{\alpha_r}), \max(|z_1|, \dots, |z_r|) \rightarrow 0$$

$$\aleph(z_1, \dots, z_r) = O(|z_1|^{\beta_1}, \dots, |z_r|^{\beta_r}), \min(|z_1|, \dots, |z_r|) \rightarrow \infty \text{ and}$$

$$\alpha_k = \min[\operatorname{Re}(d_j^{(k)} / \delta_j^{(k)}), j = 1, \dots, M_k]$$

$$\beta_k = \max[\operatorname{Re}((c_j^{(k)} - 1) / \gamma_j^{(k)}), j = 1, \dots, N_k]$$

Series representation of Aleph-function of several variables is given by

$$\begin{aligned} \aleph(z_1, \dots, z_r) = & \sum_{G_1, \dots, G_r=0}^{\infty} \sum_{g_1=0}^{M_1} \dots \sum_{g_r=0}^{M_r} \frac{(-)^{G_1+\dots+G_r}}{\delta_{g_1}^{G_1} \dots \delta_{g_r}^{G_r}} \psi(\eta_{G_1, g_1}, \dots, \eta_{G_r, g_r}) \\ & \times \theta_1(\eta_{G_1, g_1}) \dots \theta_r(\eta_{G_r, g_r}) z_1^{-\eta_{G_1, g_1}} \dots z_r^{-\eta_{G_r, g_r}} \end{aligned} \quad (1.6)$$

Where $\psi(\dots), \theta_i(\dots), i = 1, \dots, r$ are given respectively in (1.2), (1.3) and

$$\eta_{G_1, g_1} = \frac{d_{g_1}^{(1)} + G_1}{\delta_{g_1}^{(1)}}, \dots, \eta_{G_r, g_r} = \frac{d_{g_r}^{(r)} + G_r}{\delta_{g_r}^{(r)}}$$

$$\text{which is valid under the conditions } \delta_{g_i}^{(i)} [d_j^i + p_i] \neq \delta_j^{(i)} [d_{g_i}^i + G_i] \quad (1.7)$$

$$\text{for } j \neq M_i, M_i = 1, \dots, \eta_{G_i, g_i}; P_i, N_i = 0, 1, 2, \dots, ; y_i \neq 0, i = 1, \dots, r \quad (1.8)$$

In the document, we will note:

$$G(\eta_{G_1, g_1}, \dots, \eta_{G_r, g_r}) = \phi(\eta_{G_1, g_1}, \dots, \eta_{G_r, g_r}) \theta_1(\eta_{G_1, g_1}) \dots \theta_r(\eta_{G_r, g_r}) \quad (1.9)$$

where $\phi(\eta_{G_1, g_1}, \dots, \eta_{G_r, g_r}), \theta_1(\eta_{G_1, g_1}), \dots, \theta_r(\eta_{G_r, g_r})$ are given respectively in (1.2) and (1.3)

$$\text{We will note the Aleph-function of } r \text{ variables } \aleph_{u:w}^{0,N:v} \left(\begin{matrix} z_1 \\ \dots \\ z_r \end{matrix} \right) \quad (1.10)$$

The multivariable I-function is defined in term of multiple Mellin-Barnes type integral:

$$\begin{aligned} I(z_1, z_2, \dots, z_s) = & I_{p_2, q_2; p_3, q_3; \dots; p_s, q_s; p', q'; \dots; p^{(s)}, q^{(s)}}^{0, n_2; 0, n_3; \dots; 0, n_r; m', n'; \dots; m^{(s)}, n^{(s)}} \left(\begin{matrix} z_1 \\ \cdot \\ \cdot \\ \cdot \\ z_s \end{matrix} \middle| \begin{matrix} (a_{2j}; \alpha'_{2j}, \alpha''_{2j})_{1, p_2}; \dots; \\ (b_{2j}; \beta'_{2j}, \beta''_{2j})_{1, q_2}; \dots; \end{matrix} \right) \\ & \left(\begin{matrix} (a_{sj}; \alpha'_{sj}, \dots, \alpha_{sj}^{(s)})_{1, p_s}; (a'_j, \alpha'_j)_{1, p'}; \dots; (a_j^{(s)}, \alpha_j^{(s)})_{1, p^{(s)}} \\ (b_{sj}; \beta'_{sj}, \dots, \beta_{sj}^{(s)})_{1, q_s}; (b'_j, \beta'_j)_{1, q'}; \dots; (b_j^{(s)}, \beta_j^{(s)})_{1, q^{(s)}} \end{matrix} \right) \end{aligned} \quad (1.11)$$

$$= \frac{1}{(2\pi\omega)^s} \int_{L_1} \cdots \int_{L_s} \xi(t_1, \dots, t_s) \prod_{i=1}^s \phi_i(t_i) z_i^{t_i} dt_1 \cdots dt_s \quad (1.12)$$

The defined integral of the above function, the existence and convergence conditions, see Y,N Prasad [4]. Throughout the present document, we assume that the existence and convergence conditions of the multivariable I-function.

The condition for absolute convergence of multiple Mellin-Barnes type contour (1.9) can be obtained by extension of the corresponding conditions for multivariable H-function given by as :

$$|arg z_k| < \frac{1}{2} \Omega_i^{(k)} \pi, \text{ where}$$

$$\begin{aligned} \Omega_i^{(k)} = & \sum_{k=1}^{n^{(i)}} \alpha_k^{(i)} - \sum_{k=n^{(i)}+1}^{p^{(i)}} \alpha_k^{(i)} + \sum_{k=1}^{m^{(i)}} \beta_k^{(i)} - \sum_{k=m^{(i)}+1}^{q^{(i)}} \beta_k^{(i)} + \left(\sum_{k=1}^{n_2} \alpha_{2k}^{(i)} - \sum_{k=n_2+1}^{p_2} \alpha_{2k}^{(i)} \right) + \cdots + \\ & \left(\sum_{k=1}^{n_s} \alpha_{sk}^{(i)} - \sum_{k=n_s+1}^{p_s} \alpha_{sk}^{(i)} \right) - \left(\sum_{k=1}^{q_2} \beta_{2k}^{(i)} + \sum_{k=1}^{q_3} \beta_{3k}^{(i)} + \cdots + \sum_{k=1}^{q_s} \beta_{sk}^{(i)} \right) \end{aligned} \quad (1.13)$$

where $i = 1, \dots, s$

The complex numbers z_i are not zero. Throughout this document, we assume the existence and absolute convergence conditions of the multivariable I-function.

We may establish the the asymptotic expansion in the following convenient form :

$$I(z_1, \dots, z_s) = O(|z_1|^{\alpha'_1}, \dots, |z_s|^{\alpha'_s}), \max(|z_1|, \dots, |z_s|) \rightarrow 0$$

$$I(z_1, \dots, z_s) = O(|z_1|^{\beta'_1}, \dots, |z_s|^{\beta'_s}), \min(|z_1|, \dots, |z_s|) \rightarrow \infty$$

where, with $k = 1, \dots, s : \alpha'_k = \min[Re(b_j^{(k)})/\beta_j^{(k)}], j = 1, \dots, m_k$ and

$$\beta'_k = \max[Re((a_j^{(k)} - 1)/\alpha_j^{(k)}), j = 1, \dots, n_k$$

We will use these following notations in this paper :

$$U = p_2, q_2; p_3, q_3; \cdots; p_{s-1}, q_{s-1}; V = 0, n_2; 0, n_3; \cdots; 0, n_{s-1} \quad (1.14)$$

$$W = (p', q'); \cdots; (p^{(s)}, q^{(s)}); X = (m', n'); \cdots; (m^{(s)}, n^{(s)}) \quad (1.15)$$

$$A = (a_{2k}, \alpha'_{2k}, \alpha''_{2k}); \cdots; (a_{(s-1)k}, \alpha'_{(s-1)k}, \alpha''_{(s-1)k}, \cdots, \alpha^{(s-1)}_{(s-1)k}) \quad (1.16)$$

$$B = (b_{2k}, \beta'_{2k}, \beta''_{2k}); \cdots; (b_{(s-1)k}, \beta'_{(s-1)k}, \beta''_{(s-1)k}, \cdots, \beta^{(s-1)}_{(s-1)k}) \quad (1.17)$$

$$\mathfrak{A} = (a_{sk}; \alpha'_{sk}, \alpha''_{sk}, \cdots, \alpha^s_{sk}) : \mathfrak{B} = (b_{sk}; \beta'_{sk}, \beta''_{sk}, \cdots, \beta^s_{sk}) \quad (1.18)$$

$$A' = (a'_k, \alpha'_k)_{1,p'}; \dots; (a_k^{(s)}, \alpha_k^{(s)})_{1,p^{(s)}}; B' = (b'_k, \beta'_k)_{1,p'}; \dots; (b_k^{(s)}, \beta_k^{(s)})_{1,p^{(s)}} \quad (1.19)$$

The multivariable I-function write :

$$I(z_1, \dots, z_s) = I_{U:p_s, q_s; W}^{V; 0, n_s; X} \left(\begin{array}{c} z_1 \\ \cdot \\ \cdot \\ \cdot \\ z_s \end{array} \middle| \begin{array}{l} A; \mathfrak{A}; A' \\ \\ \\ B; \mathfrak{B}; B' \end{array} \right) \quad (1.20)$$

The generalized polynomials defined by Srivastava [6], is given in the following manner :

$$S_{N'_1, \dots, N'_t}^{M'_1, \dots, M'_t} [y_1, \dots, y_t] = \sum_{K_1=0}^{[N'_1/M'_1]} \dots \sum_{K_t=0}^{[N'_t/M'_t]} \frac{(-N'_1)_{M'_1 K_1}}{K_1!} \dots \frac{(-N'_t)_{M'_t K_t}}{K_t!} A[N'_1, K_1; \dots; N'_t, K_t] y_1^{K_1} \dots y_t^{K_t} \quad (1.21)$$

Where M'_1, \dots, M'_t are arbitrary positive integers and the coefficients $A[N'_1, K_1; \dots; N'_t, K_t]$ are arbitrary constants, real or complex. In the present paper, we use the following notation

$$a_1 = \frac{(-N'_1)_{M'_1 K_1}}{K_1!} \dots \frac{(-N'_t)_{M'_t K_t}}{K_t!} A[N'_1, K_1; \dots; N'_t, K_t] \quad (1.22)$$

2. Generalized multiple-index Mittag-Leffler function

A further generalization of the Mittag-Leffler functions is proposed recently in Paneva-Konovska [2]. These are 3m-parametric Mittag-Leffler type functions generalizing the Prabhakar [3] 3-parametric function , defined as:

$$E_{(\alpha_i), (\beta_i)}^{(\gamma_i), m}(z) = \sum_{k=0}^{\infty} \frac{(\gamma_1)_k \dots (\gamma_m)_k}{\Gamma(\alpha_1 k + \beta_1) \dots \Gamma(\alpha_m k + \beta_m)} \frac{z^k}{k!} \quad (2.1)$$

where $\alpha_i, \beta_i, \gamma_i \in \mathbb{C}, i = 1, \dots, m, \text{Re}(\alpha_i) > 0$

3. Required formula

We have the following multiple integral transformation, see Marichev et al ([1], 33.5 11 page 595).

$$\int_0^1 \dots \int_0^1 f(x_1 \dots x_n) (1-x_1)^{v_1-1} \prod_{i=2}^n x_i^{v_1+\dots+v_i-1} (1-x_i)^{v_i-1} dx_1 \dots dx_n \\ = \frac{\Gamma(v_1) \dots \Gamma(v_n)}{\Gamma(v_1 + \dots + v_n)} \times \int_0^1 f(x) (1-x)^{v_1+\dots+v_n-1} dx \quad (3.1)$$

where $v_i > 0, i = 1, \dots, n$, provided that the integral of the right hand side converges absolutely.

4. Main integral

We note : $X_{v_1, \dots, v_n} = (1 - x_1)^{v_1} \prod_{l=2}^n x_l^{v_1 + \dots + v_l} (1 - x_l)^{v_l}$ and $b_k = \frac{(\gamma_1)_k \dots (\gamma_m)_k}{\Gamma(\alpha_1 k + \beta_1) \dots \Gamma(\alpha_m k + \beta_m)}$

and we have the following formula :

$$\int_0^1 \dots \int_0^1 f(x_1 \dots x_n) (1 - x_1)^{v_1} \prod_{l=2}^n x_l^{v_1 + \dots + v_l} (1 - x_l)^{v_l - 1} E_{(\alpha_i), (\beta_i)}^{(\gamma_i), m}(z X_{\xi_1, \dots, \xi_n})$$

$$S_{N_1, \dots, N_t}^{M'_1, \dots, M'_t} \left(\begin{matrix} y_1 X_{\gamma_1^{(1)}, \dots, \gamma_1^{(n)}} \\ \dots \\ y_t X_{\gamma_t^{(1)}, \dots, \gamma_t^{(n)}} \end{matrix} \right) N_{u:w}^{0, N; v} \left(\begin{matrix} z_1 X_{\alpha_1^{(1)}, \dots, \alpha_1^{(n)}} \\ \dots \\ z_r X_{\alpha_r^{(1)}, \dots, \alpha_r^{(n)}} \end{matrix} \right) I_{U: p_s, q_s; W}^{V; 0, n_s; X} \left(\begin{matrix} Z_1 X_{\eta_1^{(1)}, \dots, \eta_1^{(n)}} \\ \dots \\ Z_s X_{\eta_s^{(1)}, \dots, \eta_s^{(n)}} \end{matrix} \right) dx_1 \dots dx_n$$

$$= \sum_{K_1=0}^{[N'_1/M'_1]} \dots \sum_{K_t=0}^{[N'_t/M'_t]} \sum_{k=0}^{\infty} \sum_{G_1, \dots, G_r=0}^{\infty} \sum_{g_1=0}^{M_1} \dots \sum_{g_r=0}^{M_r} \frac{(-)^{G_1 + \dots + G_r}}{\delta_{g_1} G_1! \dots \delta_{g_r} G_r!} G(\eta_{G_1, g_1}, \dots, \eta_{G_r, g_r}) a_1 \frac{b_k z^k}{k!}$$

$$z_1^{\eta_{G_1, g_1}} \dots z_r^{\eta_{G_r, g_r}} y_1^{K_1} \dots y_t^{K_t} \int_0^1 (1 - x)^{\sum_{i=1}^n (k \xi_i + \sum_{j=1}^t K_j \gamma_j^{(i)} + \sum_{j=1}^r \eta_{G_j, g_j} \alpha_j^{(i)}) - 1} f(x)$$

$$I_{U: p_s + n, q_s + 1; W}^{V; 0, n_s + n; X} \left(\begin{matrix} Z_1 (1 - x)^{\eta_1^{(1)} + \dots + \eta_1^{(n)}} \\ \dots \\ Z_s (1 - x)^{\eta_s^{(1)} + \dots + \eta_s^{(n)}} \end{matrix} \middle| \begin{matrix} A; \\ B; \end{matrix} \right)$$

$$\left[1 - (v_i + k \xi_i + \sum_{j=1}^t K_j \gamma_j^{(i)} + \sum_{j=1}^r \eta_{G_j, g_j} \alpha_j^{(i)}); \eta_1^{(i)}, \dots, \eta_s^{(i)} \right]_{1, n}, \mathfrak{A}; A' \left. \begin{matrix} \dots \\ B_1, \mathfrak{B}; B' \end{matrix} \right) dx \quad (4.1)$$

$$\text{where : } B_1 = \left\{ 1 - \sum_{i=1}^n \left[v_i + k \xi_i + \sum_{j=1}^t K_j \gamma_j^{(i)} + \sum_{j=1}^r \eta_{G_j, g_j} \alpha_j^{(i)} \right] ; \eta_1^{(1)} + \dots + \eta_1^{(n)}, \right.$$

$$\left. \dots, \eta_s^{(1)} + \dots + \eta_s^{(n)} \right\} \quad (4.2)$$

Provided that

a) $\min\{\xi_i, v_i, \gamma_j^{(i)}, \alpha_k^{(i)}, \eta_l^{(i)}\} > 0, i = 1, \dots, n, j = 1, \dots, t, k = 1, \dots, r, l = 1, \dots, s$

b) $Re[v_i + k\xi_i + \sum_{j=1}^r \alpha_j^{(i)} \min_{1 \leq j \leq M_i} \frac{d_j^{(i)}}{\delta_j^{(i)}} + \sum_{j=1}^s \eta_j^{(i)} \min_{1 \leq j \leq m_i} \frac{b_j^{(i)}}{\beta_j^{(i)}}] > 0, i = 1, \dots, n$

c) $|arg z_k| < \frac{1}{2} A_i^{(k)} \pi$, where $A_i^{(k)}$ is defined by (1.5); $i = 1, \dots, r$

d) $|arg Z_k| < \frac{1}{2} \Omega_i^{(k)} \pi$, where $\Omega_i^{(k)}$ is defined by (1.11); $i = 1, \dots, s$

e) $\alpha_i, \beta_i, \gamma_i \in \mathbb{C}, i = 1, \dots, m, Re(\alpha_i) > 0$

f) The integral of the right hand side converges absolutely.

g) The series occurring on the right-hand side of (4.1) is absolutely and uniformly convergent.

The quantities $U, V, W, X, A, B, \mathfrak{A}, \mathfrak{B}, A'$ and B' are defined by the equations (1.14) to (1;19)

Proof of (4.1) : Let $M = \frac{1}{(2\pi\omega)^s} \int_{L_1} \dots \int_{L_s} \xi(t_1, \dots, t_s) \prod_{i=1}^s \phi_i(t_i)$. We have :

$$E_{(\alpha_i), (\beta_i)}^{(\gamma_i), m} (z X_{\xi_1, \dots, \xi_n}) S_{N_1, \dots, N_t}^{M'_1, \dots, M'_t} \begin{pmatrix} y_1 X_{\gamma_1^{(1)}, \dots, \gamma_1^{(n)}} \\ \dots \\ y_t X_{\gamma_t^{(1)}, \dots, \gamma_t^{(n)}} \end{pmatrix} X_{u:w}^{0, N:v} \begin{pmatrix} z_1 X_{\alpha_1^{(1)}, \dots, \alpha_1^{(n)}} \\ \dots \\ z_r X_{\alpha_r^{(1)}, \dots, \alpha_r^{(n)}} \end{pmatrix}$$

$$I_{U:p_s, q_s; W}^{V:0, n_s; X} \begin{pmatrix} Z_1 X_{\eta_1^{(1)}, \dots, \eta_1^{(n)}} \\ \dots \\ Z_s X_{\eta_s^{(1)}, \dots, \eta_s^{(n)}} \end{pmatrix} \sum_{G_1, \dots, G_r=0}^{\infty} \sum_{g_1=0}^{M_1} \dots \sum_{g_r=0}^{M_r} \sum_{K_1=0}^{[N'_1/M'_1]} \dots \sum_{K_t=0}^{[N'_t/M'_t]} \sum_{k=0}^{\infty} \frac{(-)^{G_1+\dots+G_r}}{\delta_{g_1} G_1! \dots \delta_{g_r} G_r!}$$

$$G(\eta_{G_1, g_1}, \dots, \eta_{G_r, g_r}) a_1 \frac{b_k z^k}{k!} z_1^{\eta_{G_1, g_1}} \dots z_r^{\eta_{G_r, g_r}} y_1^{K_1} \dots y_t^{K_t} \prod_{j=1}^t X_{\gamma_j^{(1)}, \dots, \gamma_j^{(n)}}^{K_j} X_{\xi(1), \dots, \xi(n)}^k \prod_{j=1}^r X_{\alpha_j^{(1)}, \dots, \alpha_j^{(n)}}^{\eta_{G_j, g_j}}$$

$$M \left[\prod_{j=1}^s Z^j X_{\eta_j^{(1)}, \dots, \eta_j^{(n)}}^{t_j} \right] dt_1 \dots dt_s \tag{4.3}$$

Multiplying both sides of (4.3) by $f(x_1 \dots x_n) (1-x_1)^{v_1} \prod_{l=2}^n x_l^{v_1+\dots+v_l} (1-x_l)^{v_l-1}$ and integrating with respect to x_1, \dots, x_s verifying the conditions e), changing the order of integration and summation (which is easily seen to be justified due to the absolute convergence of the integral and the summations involved in the process), we obtain :

$$\sum_{G_1, \dots, G_r=0}^{\infty} \sum_{g_1=0}^{M_1} \dots \sum_{g_r=0}^{M_r} \sum_{K_1=0}^{[N'_1/M'_1]} \dots \sum_{K_t=0}^{[N'_t/M'_t]} \sum_{k=0}^{\infty} \frac{(-)^{G_1+\dots+G_r}}{\delta_{g_1} G_1! \dots \delta_{g_r} G_r!} G(\eta_{G_1, g_1}, \dots, \eta_{G_r, g_r}) a_1 \frac{b_k z^k}{k!}$$

$$z_1^{\eta_{G_1, g_1}} \dots z_r^{\eta_{G_r, g_r}} y_1^{K_1} \dots y_t^{K_t} \int_0^1 \dots \int_0^1 \prod_{j=1}^t X_{\gamma_j^{(1)}, \dots, \gamma_j^{(n)}}^{K_j} X_{\xi_1, \dots, \xi_n}^k \prod_{j=1}^r X_{\alpha_j^{(1)}, \dots, \alpha_j^{(n)}}^{\eta_{G_j, g_j}}$$

$$\left\{ M \left[\prod_{j=1}^s Z_j X_{\eta_j^{(1)}, \dots, \eta_j^{(n)}}^{t_j} \right] dt_1 \dots dt_s \right\} f(x_1 \dots x_n) (1-x_1)^{v_1} \prod_{l=2}^n x_l^{v_1+\dots+v_l} (1-x_l)^{v_l-1}$$

$$dx_1 \dots dx_n \tag{4.4}$$

Change the order of the (x_1, \dots, x_n) -integral and (t_1, \dots, t_s) -integral, we get :

$$\sum_{G_1, \dots, G_r=0}^{\infty} \sum_{g_1=0}^{M_1} \dots \sum_{g_r=0}^{M_r} \sum_{K_1=0}^{[N'_1/M'_1]} \dots \sum_{K_t=0}^{[N'_t/M'_t]} \sum_{k=0}^{\infty} \frac{(-)^{G_1+\dots+G_r}}{\delta_{g_1} G_1! \dots \delta_{g_r} G_r!} G(\eta_{G_1, g_1}, \dots, \eta_{G_r, g_r}) a_1 \frac{b_k z^k}{k!}$$

$$z_1^{\eta_{G_1, g_1}} \dots z_r^{\eta_{G_r, g_r}} y_1^{K_1} \dots y_t^{K_t} M \left\{ \prod_{j=1}^s Z_j^{t_j} \int_0^1 \dots \int_0^1 (1-x_1)^{v_1+\xi_1 k + \sum_{j=1}^t K_j \gamma_j^{(1)} + \sum_{j=1}^r \eta_{G_j, g_j} \alpha_j^{(1)} + \sum_{j=1}^s t_j \eta_j^{(1)}} \right.$$

$$\left. \prod_{l=2}^n (1-x_l)^{v_l+k\xi_l + \sum_{j=1}^t K_j \gamma_j^{(l)} + \sum_{j=1}^r \eta_{G_j, g_j} \alpha_j^{(l)} + \sum_{j=1}^s t_j \eta_j^{(l)}} - 1 \right\} f(x_1 \dots x_n)$$

$$\left. \prod_{l=2}^n x_l^{\sum_{i=1}^s (\xi_i k + \sum_{j=1}^t K_j \gamma_j^{(i)} + \sum_{j=1}^r \eta_{G_j, g_j} \alpha_j^{(i)} + \sum_{j=1}^s t_j \eta_j^{(i)} + v_i)} dx_1 \dots dx_n \right] dt_1 \dots dt_s \tag{4.5}$$

Use the equation (3.1) and interpreting the result thus obtained with the Mellin-barnes contour integral (1.12), we arrive at the desired result.

5. Particular case

If $U = V = A = B = 0$, the multivariable I-function defined by Prasad degenerates in multivariable H-function defined by Srivastava et al [7]. We have the following result.

Lemme

$$\int_0^1 \dots \int_0^1 f(x_1 \dots x_n) (1-x_1)^{v_1-1} \prod_{i=2}^n x_i^{v_1+\dots+v_i-1} (1-x_i)^{v_i-1} E_{(\alpha_i), (\beta_i)}^{(\gamma_i), m}(z X_{\xi_1, \dots, \xi_n})$$

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